HAMPI: A Solver for Word Equations over Strings, Regular Expressions, and Context-Free Grammars

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Many automatic testing, analysis, and verification techniques for programs can be effectively reduced to a constraint-generation phase followed by a constraint-solving phase. This separation of concerns often leads to more effective and maintainable software reliability tools. The increasing efficiency of off-the-shelf constraint solvers makes this approach even more compelling. However, there are few effective and sufficiently expressive off-the-shelf solvers for string constraints generated by analysis of string-manipulating programs, so researchers end up implementing their own ad-hoc solvers.

To fulfill this need, we designed and implemented HAMPI, a solver for string constraints over bounded string variables. Users of HAMPI specify constraints using regular expressions, context-free grammars, equality between string terms, and typical string operations such as concatenation and substring extraction. HAMPI then finds a string that satisfies all the constraints or reports that the constraints are unsatisfiable.

We demonstrate HAMPI's expressiveness and efficiency by applying it to program analysis and automated testing. We used HAMPI in static and dynamic analyses for finding SQL injection vulnerabilities in Web applications with hundreds of thousands of lines of code. We also used HAMPI in the context of automated bug finding in C programs using dynamic systematic testing (also known as concolic testing). We then compared HAMPI with another string solver, CFGAnalyzer, and show that HAMPI is several times faster. HAMPI's source code, documentation, and experimental data are available at `http://people.csail.mit.edu/akiezun/hampi`[1].

1. INTRODUCTION

Many automatic testing [Cadar et al. 2006; Sen et al. 2005; Godefroid et al. 2005], analysis [Gulwani et al. 2008; Xie and Aiken 2005], and verification [Jackson and Vaziri 2000; Clarke et al. 2004] techniques for programs can be effectively reduced to a constraint-generation phase followed by a constraint-solving phase. This separation of concerns often leads to more effective and maintainable tools. Such an approach to analyzing programs is becoming more effective as the efficiency of off-the-shelf constraint solvers for Boolean SAT [Moskewicz et al. 2001] and other theories [de Moura and Bjørner 2008; Ganesh and Dill 2007] continues to increase. Most of these solvers are aimed at propositional logic, linear arithmetic, or the theory of bit-vectors.

Many programs (e.g., Web applications) take string values as input, manipulate them, and then use them in sensitive operations such as database queries. Analyses of string-manipulating programs in techniques for automatic testing [Emmi et al. 2007; Godefroid et al. 2008a; Bjørner et al. 2009], verifying correctness of program output [Shannon et al. 2007], and finding security faults [Fu et al. 2007; Wassermann et al. 2008] produce *string constraints*, which are then solved by custom string solvers written by the authors of these analyses. Writing a custom solver for every application is time-consuming and error-prone, and the lack of separation of concerns may lead to systems that are difficult to maintain. Thus, there is a clear need for an effective and sufficiently expressive off-the-shelf string-constraint solver that can be easily integrated into a variety of applications.

To fulfill this need, we designed and implemented HAMPI, a solver for constraints over bounded string variables. HAMPI constraints express membership in bounded regular and context-free languages, substring relations, and equalities/disequalities over string terms.

String terms in the HAMPI language are constructed out of string constants, bounded string variables, concatenation, and extraction operations. Regular expressions and context-free grammar terms are constructed out of standard regular expression operations and grammar productions, respectively. Atomic formulas in the HAMPI language are equality over string terms, the membership predicate for regular expressions and context-free grammars, and the substring predicate that takes two string terms and asserts that one is a substring of the other. Given a set of constraints, HAMPI outputs a string that satisfies all the constraints, or reports that the constraints are unsatisfiable.

HAMPI is designed to be used as a component in testing, analysis, and verification applications. HAMPI can also be used to solve the intersection, containment, and equivalence problems for bounded regular and context-free languages.

A key feature of HAMPI is bounding of regular and context-free languages. Bounding makes HAMPI different from custom string-constraint solvers commonly used in testing and analysis tools [Emmi et al. 2007]. As we demonstrate in our experiments, for many practical applications, bounding the input languages is not a handicap. In fact, it allows for a more expressive input language that enables operations on context-free languages that would be undecidable without bounding. Furthermore, bounding makes the satisfiability problem solved by HAMPI more tractable. This difference is analogous to that between model-checking and bounded model-checking [Biere et al. 2003].

As one example application, HAMPI's input language can encode constraints on SQL queries to find possible injection attacks, such as:

> Find a string v of at most 12 characters, such that the SQL query "`SELECT msg FROM messages WHERE topicid=`v" is a syntactically valid SQL statement, and that the query contains the substring "`OR 1=1`".

Note that "OR 1=1" is a common tautology that can lead to SQL injection attacks. HAMPI either finds a string value that satisfies these constraints or answers that no satisfying value exists. For the above example, the string "1 OR 1=1" is a valid solution.

HAMPI Overview. HAMPI takes four steps to solve input string constraints.

(1) Normalize the input constraints to a *core form*, which consists of expressions of the form $v \in R$ or $v \notin R$, where v is a bounded string variable, and R is a regular expression.
(2) Translate core form string constraints into a quantifier-free logic of bit-vectors. A bit-vector is a bounded, ordered list of bits. The fragment of bit-vector logic that HAMPI uses allows standard Boolean operations, bit comparisons, and extracting subvectors.
(3) Invoke the STP bit-vector solver [Ganesh and Dill 2007] on the bit-vector constraints.
(4) If STP reports that the constraints are unsatisfiable, then HAMPI reports the same. Otherwise, STP will generate a satisfying assignment in its bit-vector language, so HAMPI decodes this to output an ASCII string solution.

Experimental Results Summary. We ran four experiments to evaluate HAMPI. Our results show that HAMPI is efficient and that its input language can express string constraints that arise from real-world program analysis and automated testing tools.

(1) *SQL Injection Vulnerability Detection (static analysis).* We used HAMPI in a static analysis tool [Wassermann and Su 2007] for identifying SQL injection vulnerabilities. We applied the analysis tool to 6 PHP Web applications (total lines of code: 339,750). HAMPI solved all constraints generated by the analysis, and solved 99.7% of those constraints in less than 1 second per constraint. All solutions found by HAMPI for these constraints were less than 5 characters long. These experiments bolster our claim that bounding the string constraints is not a handicap.
(2) *SQL Injection Attack Generation (dynamic analysis).* We used HAMPI in Ardilla, a dynamic analysis tool for creating SQL injection attacks [Kiezun et al. 2009b]. We applied Ardilla to 5 PHP Web applications (total lines of code: 14,941). HAMPI successfully replaced a custom-made attack generator and constructed all 23 attacks on those applications that Ardilla originally constructed.
(3) *Input Generation for Systematic Testing.* We used HAMPI in Klee [Cadar et al. 2008], a systematic-testing tool for C programs. We used HAMPI to constrain the search space of Klee so that it could achieve higher coverage. We applied Klee to 3 programs with structured input formats (total executable lines of code: 4,100). We used HAMPI to generate constraints that specify legal inputs to these programs. HAMPI's constraints eliminated all illegal inputs, improved the line-coverage by up to $2\times$ overall (and up to $5\times$ in parsing code), and discovered 3 new error-revealing inputs.
(4) *Performance Comparison.* We compared HAMPI's performance to CFGAnalyzer, a solver for bounded versions of decision problems on context-free grammars [Axelsson et al. 2008]. HAMPI was, on average, 6.8 times faster than CFGAnalyzer on 100 grammar-intersection problems (taken randomly from a set of student submissions for verbally-described grammars).

1.1. CONTRIBUTIONS

We make the following contributions in this article.

(1) We present a *decision procedure* (solver) for constraints over bounded string variables, supporting regular language membership, context-free language membership, equality between string terms, and typical string operations.

```
1  $my_topicid = $_GET['topicid'];
2
3  $sqlstmt = "SELECT msg FROM messages WHERE topicid='$my_topicid'";
4  $result = mysql_query($sqlstmt);
5
6  //display messages
7  while($row = mysql_fetch_assoc($result)){
8    echo "Message " . $row['msg'];
9  }
```

Fig. 1. Fragment of a PHP program that displays messages stored in a MySQL database. This program is vulnerable to an SQL injection attack. Section 2 discusses the vulnerability.

(2) We introduce HAMPI, an open-source implementation of the decision procedure. HAMPI's format for context-free grammars and regular expressions is as expressive as that of widely-used tools such as Yacc/Lex; in fact, we have written a script that transforms a Yacc specification to HAMPI format. Also, our colleague Devdatta Akhave wrote a script that translates Perl Compatible Regular Expressions (PCRE) into HAMPI format. HAMPI's source code, documentation, and supporting scripts are available at: `http://people.csail.mit.edu/akiezun/hampi`.
(3) We provide an Experimental evaluation of HAMPI for program analysis, security, and automated testing applications.
(4) We provide experimental data (downloadable from HAMPI's Web site) that can be used as benchmarks for developing and evaluating future string solvers.
(5) We also made significant improvements over an earlier 2009 version of HAMPI, described in the following text.

Improvements over 2009 version of HAMPI. We published the first version of HAMPI in an ISSTA 2009 conference paper [Kiezun et al. 2009a]. In the past two years, we have made the following significant improvements to HAMPI's expressiveness based on the needs of our users.

(1) HAMPI now automatically infers size bounds for language-membership constraints. The previous version of HAMPI required the user to calculate a size bound to convert a context-free language into a regular language.
(2) HAMPI now supports word equations (equalities and disequalities) over string terms.
(3) HAMPI now allows variable-sized strings to be declared.
(4) HAMPI now supports a substring extraction operation.
(5) HAMPI now allows multiple input string variables, simulating this feature by using a single long bounded string variable and the extraction operation.

1.2. ARTICLE ORGANIZATION

We first introduce HAMPI's capabilities with an example (Section 2), then present HAMPI's input format and solving algorithm (Section 3), discuss speed optimizations (Section 4), and present experimental evaluation (Section 5). We end with related work (Section 6) and conclusion (Section 7).

2. EXAMPLE: SQL INJECTION

SQL injections are a prevalent class of Web-application vulnerabilities. This section illustrates how an automated tool [Kiezun et al. 2009b; Wassermann et al. 2008] could use HAMPI to detect SQL injection vulnerabilities and to produce attack inputs.

Figure 1 shows a fragment of a PHP program that implements a simple Web application: a message board that allows users to read and post messages stored in a

```
1  //string variable representing '$my_topicid' from Figure 1
2  var v:6..12;    // size is between 6 and 12 characters
3
4  //simple SQL context-free grammar
5  cfg SqlSmall := "SELECT " (Letter)+ " FROM " (Letter)+ " WHERE " Cond;
6  cfg Cond      := Val "=" Val | Cond " OR " Cond";
7  cfg Val       := (Letter)+ | "'" (LetterOrDigit)* "'" | (Digit)+;
8  cfg LetterOrDigit := Letter | Digit;
9  cfg Letter := ['a'-'z'] ;
10 cfg Digit  := ['0'-'9'] ;
11
12 //the SQL query $sqlstmt from line 3 of Figure 1
13 val q := concat("SELECT msg FROM messages WHERE topicid='", v, "'");
14
15 //constraint conjuncts
16 assert q in SqlSmall;
17 assert q contains "OR '1'='1'";
```

Fig. 2. HAMPI input that, when solved, produces an SQL injection attack vector for the vulnerability from Figure 1.

MySQL database. Users of the message board fill in an HTML form (not shown here) that communicates the inputs to the server via a specially formatted URL, for instance, `http://www.mysite.com/?topicid=1`. Input parameters passed inside the URL are available in the $_GET associative array. In the above example URL, the input has one key-value pair: `topicid=1`. The program fragment in Figure 1 retrieves and displays messages for the given topic.

This program is vulnerable to an SQL injection attack. An attacker can read all messages in the database (including ones intended to be private) by crafting a malicious URL like:

`http://www.mysite.com/?topicid=1' OR '1'='1`.

Upon being invoked with that URL, the program reads the string

`1' OR '1'='1`

as the value of the $my_topicid variable, constructs an SQL query by concatenating it to a constant string, and submits the following query to the database in line 4.

`SELECT msg FROM messages WHERE topicid='1' OR '1'='1'`

The WHERE condition is always true because it contains the tautology '1'='1'. Thus, the query retrieves all messages, possibly leaking private information.

A programmer or an automated tool might ask, "Can an attacker exploit the topicid parameter and introduce a OR '1'='1' tautology into a syntactically correct SQL query at line 4 in the code of Figure 1?" The HAMPI solver is designed to help answer such questions and serve as a back-end solver in an automated analysis tool to create strings that can be used as exploits.

The HAMPI constraints in Figure 2 formalize the question in our example. Automated vulnerability-scanning tools [Kiezun et al. 2009b; Wassermann et al. 2008] can create HAMPI constraints via either static or dynamic program analysis (we demonstrate both static and dynamic techniques in our evaluation in Sections 5.1 and 5.2, respectively). Specifically, a tool could create the HAMPI input shown in Figure 2 by analyzing the code of Figure 1.
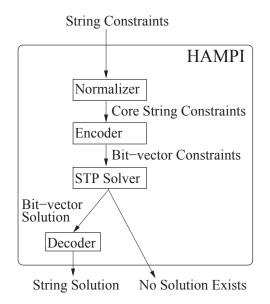
Fig. 3. Schematic view of the HAMPI string constraint solver. Input enters at the top, and output exits at the bottom. Section 3 describes the HAMPI solver.

We now discuss various features of the HAMPI input language that Figure 2 illustrates. (Section 3.1 describes the input language in more detail.)

—Keyword var (line 2) introduces a *string variable* v. The variable has a size in the range of 6 to 12 characters. The goal of the HAMPI solver is to find a string that, when assigned to the string variable, satisfies all the constraints. In this example, HAMPI will search for solutions of sizes between 6 and 12.
—Keyword cfg (lines 5–10) introduces a *context-free grammar*, for a fragment of the SQL grammar of SELECT statements.
—Keyword val (line 13) introduces a temporary variable q, declared as a *concatenation* of constant strings and the string variable v. This variable represents an SQL query corresponding to the PHP $sqlstmt variable from line 3 in Figure 1.
—Keyword assert defines a constraint. The top-level HAMPI constraint is a conjunction of assert statements. Line 16 specifies that the query string q must be a member of the context-free language SqlSmall (syntactically-correct SQL). Line 17 specifies that the variable v must contain a specific substring (e.g., the OR '1'='1' tautology that can lead to an SQL injection attack).

HAMPI can solve the constraints specified in Figure 2 and find a value for v such as

    1' OR '1'='1,

which is a value for $_GET['topicid'] that can lead to an SQL injection attack.

3. THE HAMPI STRING CONSTRAINT SOLVER

HAMPI finds a string that satisfies constraints specified in the input, or decides that no satisfying string exists. HAMPI works in four steps, as illustrated in Figure 3.

(1) Normalize the input constraints to a *core form* (Section 3.2).
(2) Encode core form constraints in bit-vector logic (Section 3.3).

Input	::=	*Var Stmt*∗	HAMPI input (with a single string variable)
Var	::=	**var** *Id* : *Int..Int*	string variable (with length lower..upper bound)
Stmt	::=	*Cfg* | *Reg* | *Val* | *Assert*	statement
Cfg	::=	**cfg** *Id* := *CfgProdRHS*	context-free language
CfgProdRHS	::=	*CFG declaration in EBNF*	Extended Backus-Naur Form (EBNF)
Reg	::=	**reg** *Id* := *RegElem*	regular-language
RegElem	::=	*StrConst*	string constant
	|	*Id*	variable reference
	|	**fixsize**(*Id* , *Int*)	CFG fixed-sizing
	|	**or**(*RegElem* ∗)	union
	|	**concat**(*RegElem* ∗)	concatenation
	|	**star**(*RegElem*)	Kleene star
Val	::=	**val** *Id* :=*ValElem*	temporary variable
ValElem	::=	*Id*	
	|	*StrConst*	
	|	**concat**(*ValElem* ∗)	concatenation
	|	*ValElem*[*offset* : *length*]	extraction(ValElem, offset, length)
Assert	::=	**assert** *Id* [**not**]? **in** *Reg*	regular-language membership
	|	**assert** *Id* [**not**]? **in** *Cfg*	context-free language membership
	|	**assert** *Id* [**not**]? **contains** *StrConst*	substring
	|	**assert** *Id* [**not**]? = *Id*	word equation (equality/disequality)
Id	::=	*String identifier*	
StrConst	::=	"*String literal constant*"	
Int	::=	*Nonnegative integer*	

Fig. 4.   Summary of HAMPI's input language. **Terminals** are bold-faced, *nonterminals* are italicized. A HAMPI input (*Input*) is a variable declaration, followed by a list of these statements: context-free-grammar declarations, regular-language declarations, temporary variables, and assertions.

(3) Invoke the STP solver [Ganesh and Dill 2007] on the bit-vector constraints (Section 3.3).
(4) Decode the results obtained from STP (Section 3.3).

Users can invoke HAMPI with a text-based command-line front-end (using the input grammar in Figure 4) or with a Java API to directly construct the HAMPI constraints.

3.1. Hampi Input Language for String Constraints

We now discuss the salient features of HAMPI's input language (Figure 4) and illustrate them on examples. The language is expressive enough to encode many kinds of string constraints generated by typical program analysis, and testing applications. HAMPI may also find uses in software-security applications, though its applicability to that domain may be limited due to the lack of the replace operator, often found in sanitization functions.

HAMPI's language supports declaration of bounded string variables and constants, concatenation and extraction operation over string terms, equality over string terms, regular-language operations, membership predicate, and declaration of context-free and regular languages, temporaries and constraints.

*3.1.1. Declaration of String Variable (*var *keyword).* A HAMPI input must declare a *single* string variable and specify its size range as lower and upper bounds on the number of characters. If the input constraints are satisfiable, then HAMPI finds a value for the

variable that satisfies all constraints. For example, the following line declares a string variable named v with a size between 5 and 20 characters.

```
var v:5..20;
```

3.1.2. Extraction Operation. HAMPI supports extraction of substrings from string terms (as shown in Figure 4). An example of extraction operation is as follows.

```
var longv:20;
val v1 := longv[0:9];
```

where 0 is the offset (or starting character of the extraction operation), and 9 is the length of the resultant string, in terms of the number of characters of *longv*.

3.1.3. Declaration of Multiple Variables. The user can simulate having multiple variables by declaring a single long string variable and using the extract operation: Disjoint extractions of the single long variable can act as multiple variables. For example, to declare two string variables of length 10 named v1 and v2, use the following.

```
var longv:20;
val v1 := longv[0:9];
val v2 := longv[10:9];
```

The val keyword declares a temporary (derived) variable and will be described later in this section.

3.1.4. Declarations of Context-Free Languages (cfg keyword). HAMPI input can declare context-free languages using grammars in the standard notation: Extended Backus-Naur Form (EBNF). Terminals are enclosed in double quotes (e.g., "SELECT"), and productions are separated by the vertical bar symbol (|). Grammars may contain special symbols for repetition (+ and *) and character ranges (e.g., [a-z]). For example, lines 5–10 in Figure 2 show the declaration of a context-free grammar for a subset of SQL.

HAMPI's format for context-free grammars is as expressive as that of widely-used tools such as Yacc/Lex; in fact, we have written a simple syntax-driven script that transforms a Yacc specification to HAMPI format (available on the HAMPI website).

HAMPI can only solve constraints over bounded context-free grammars. However, the user does not have to manually specify bounds, since HAMPI automatically derives a bound by analyzing the bound on the input string variable and the longest possible string that can be constructed out of concatenation and extraction operations.

3.1.5. Declarations of Regular Languages (reg keyword). HAMPI input can declare regular languages using the following regular expressions: (i) a singleton set with a string constant, (ii) a concatenation/union of regular languages, (iii) a repetition (Kleene star) of a regular language, (iv) bounding of a context-free language, which HAMPI does automatically. Every regular language can be expressed using the first three of those operations [Sipser 2005].

For example, (b*ab*ab*)* is a regular expression that describes the language of strings over the alphabet {a,b}, with an even number of a symbols. In HAMPI syntax this is the following.

```
reg Bstar := star("b");          // 'helper' expression
reg EvenA := star(concat(Bstar, "a", Bstar, "a", Bstar));
```

The HAMPI website contains a script to convert Perl Compatible Regular Expressions (PCRE) into HAMPI syntax.

Also note that context-free grammars in HAMPI are implicitly bounded, and hence are regular expressions.

3.1.6. Temporary Declarations (`val` keyword). Temporary variables are shortcuts for expressing constraints on expressions that are concatenations of the string variable and constants or extractions. For example, line 13 in Figure 2 declares a temporary variable named q by concatenating two constant strings to the variable v.

```
val q := concat("SELECT msg FROM messages WHERE topicid='", v, "'");
```

3.1.7. Constraints (`assert` keyword). HAMPI constraints specify membership of variables in regular and context-free languages, substrings, and word equations. HAMPI solves for the conjunction of all constraints listed in the input.

—Membership Predicate (`in`): asserts that a variable is in a context-free or regular language. For example, line 16 in Figure 2 declares that the string value of the temporary variable q is in the context-free language `SqlSmall`:

```
assert q in SqlSmall;
```

—Substring Relation (`contains`): asserts that a variable contains the given string constant. For example, line 17 in Figure 2 declares that the string value of the temporary variable q contains an SQL tautology.

```
assert q contains "OR '1'='1'";
```

—String Equalities (`=`): asserts that two string terms are equal (also known as word equations). In HAMPI, both sides of the equality must ultimately originate from the same single string variable. For example, the `extract` operator can assert that two portions of a string must be equal.

```
var v:20;
val v1 := v[0:9];
val v2 := v[10:9];
assert v1 = v2;
```

All of these constraints may be negated by preceding them with a `not` keyword.

3.2. Core Form of String Constraints

After parsing and checking the input, HAMPI normalizes the string constraints to a core form. The core form (grammar shown in Figure 5) is an internal intermediate representation that is easier than raw HAMPI input to encode in bit-vector logic.

A core form string constraint specifies membership (or its negation) in a regular language: *StrExp* $\in$ *RegExp* or *StrExp* $\notin$ *RegExp*, where *StrExp* is an expression composed of concatenations of string constants, extractions, and occurrences of the (sole) string variable, and *RegExp* is a regular expression.

HAMPI normalizes its input into core form in 3 steps.

(1) Expand all temporary variables, that is, replace each reference to a temporary variable with the variable's definition (HAMPI forbids recursive definitions of temporaries).
(2) Calculate maximum size and bound all context-free grammar expressions into regular expressions (see below for the algorithm).
(3) Expand all regular-language declarations, that is, replace each reference to a regular-language variable with the variable's definition.

$$
\begin{array}{lll}
S & ::= & Constraint \\
& | & S \wedge Constraint & \text{conjunction} \\
Constraint & ::= & StrExp \in RegExp & \text{membership} \\
& | & StrExp \notin RegExp & \text{nonmembership} \\
Constraint & ::= & StrExp = StrExp & \text{equality} \\
& | & StrExp \neq StrExp & \text{disequality} \\
StrExp & ::= & Var & \text{input variable} \\
& | & StrConst & \text{string constant} \\
& | & StrExp\ StrExp & \text{concatenation} \\
& | & StrExp[offset : length] & \text{extraction} \\
RegExp & ::= & StrConst & \text{constant} \\
& | & RegExp + RegExp & \text{union} \\
& | & RegExp\ RegExp & \text{concatenation} \\
& | & RegExp\star & \text{star}
\end{array}
$$

Fig. 5.   The grammar of core form string constraints. *Var*, *StrConst*, and *Int* are defined in Figure 4.

Fixed-sizing of Context-free Grammars. HAMPI creates regular expressions that specify the set of strings of a fixed length that are derivable from a context-free grammar. The pseudo-code of this algorithm is given as follows.

(1) Expand all special symbols in the grammar (e.g., repetition, option, character range) by adding nonterminals to the grammar and productions that correspond to the special symbols. This step is standard.
(2) Remove ϵ productions [Sipser 2005].
(3) Construct the regular expression that encodes all strings of size n that can be generated from grammar symbol S (fix(S, n)), by enumeration of all possible partitions of n characters into k grammar symbols, creating subexpressions recursively, and combining the subexpressions using concatenation operation as follows:
—fix(T, n) = T, where T is a terminal string of length n
—fix(N, n) = +(fix($S_1 \ldots S_k$, n)), union for all productions $N ::= S_1, \ldots, S_k$
—fix($S_1 \ldots S_k$, n) = +(fix($S_1 \ldots S_k$, n_1, $\ldots$, n_k)), union for all n_1, $\ldots$, n_k, such that $n_i > 0$, and $n = n_1 + \cdots + n_k$
—fix($S_1 \ldots S_k$, n_1, $\ldots$, n_k) = fix(S_1, n_1) $\ldots$ fix(S_k, n_k), concatenation of all subexpressions

HAMPI's implementation of the above algorithm uses memoization of intermediate results (Section 4.1) to make the process (worst-case exponential in k and n) scalable. Additional optimizations involve precomputing the length of the shortest and longest (if exists) string that can be generated from each nonterminal (i.e., lower and upper bounds), and using those precomputed bounds during enumeration.

Here is an example of grammar fixed-sizing: Consider the following grammar of well-balanced parentheses and the problem of finding the regular language that consists of all strings of length 6 that can be generated from the nonterminal E.

```
cfg E ::= "()" | E E | "(" E ")" ;
```

The grammar does not contain special symbols or ϵ productions, so first two steps of the algorithm do nothing. Then, HAMPI determines that the shortest string E can generate is of length 2. There are three productions for the nonterminal E, so the final regular expression is a union of three parts. The first production, E := "()", generates no strings of size 6 (and only one string of size 2). The second production, E := E E, generates strings of size 6 in two ways: either the first occurrence of E generates 2 characters and the second occurrence generates 4 characters, or the first

$$
\begin{array}{rcll}
Formula & ::= & BitVector\ =\ BitVector & \text{equality} \\
& | & Formula \lor Formula & \text{disjunction} \\
& | & Formula \land Formula & \text{conjunction} \\
& | & \neg Formula & \text{negation} \\
BitVector & ::= & Const & \text{bit-vector constant} \\
& | & Var & \text{bit-vector variable} \\
& | & Var[Int] & \text{byte extraction} \\
& | & Var[offset : length] & \text{extraction}
\end{array}
$$

Fig. 6. Grammar of bit-vector logic. Variables denote bit-vectors of fixed length. HAMPI encodes string constraints as formulas in this logic and solves using STP.

occurrence generates 4 characters and the second occurrence generates 2 characters. From the preprocessing step, HAMPI knows that the only other possible partition of 6 characters is 3–3, which HAMPI tries and fails (because E cannot generate 3-character strings). The third production, E := "(" E ")", generates strings of size 6 in only one way: the nonterminal E must generate 4 characters. In each case, HAMPI creates the subexpressions recursively. The resulting regular expression for this example is (plus signs denote union and square brackets group subexpressions).

$$()[()() + (())] \ + \ [()() + (())]() \ + \ ([()() + (())])$$

3.3. Bit-Vector Encoding and Solving

HAMPI encodes the core form string constraints as formulas in the logic of fixed-size bit-vectors. A bit-vector is a fixed-size, ordered list of bits. The fragment of bit-vector logic that HAMPI uses contains standard Boolean operations, extracting subvectors, and comparing bit-vectors (Figure 6). HAMPI asks the STP bit-vector solver [Ganesh and Dill 2007] for a satisfying assignment to the resulting bit-vector formula. If STP finds an assignment, HAMPI decodes it, and produces a string solution for the input constraints. If STP cannot find a solution, HAMPI terminates and declares the input constraints unsatisfiable.

Every core form string constraint is encoded separately, as a conjunct in a bit-vector logic formula. HAMPI encodes the core form string constraint $StrExp \in RegExp$ recursively, by case analysis of the regular expression $RegExp$, as illustrated by the following example (pseudocode shown in Figure 7).

— Consider the following HAMPI formula of the form $StrExp \in RegExp$:

$$(v) \in ()[()() + (())] \ + \ [()() + (())]() \ + \ ([()() + (())]),$$

where v is a string variable of size 4 characters, and the regular expression R_E on the right-hand side represents all balanced parantheses of exactly size 6 produced by the context-free grammar E.

```
cfg E ::= "()" | E E | "(" E ")" ;
```

— Since this regular expression R_E has only two symbols (and), it encodes constant characters using a single bit bit-vector constant where 0 represents "(", and 1 represents ")".

— A 6-bit bit-vector variable B is generated corresponding to the 6-character string (v) on the left hand side of the above formula. In addition, two new conjunctions are generated, namely, $B[0 : 1] = 0$ and $B[5 : 1] = 1$, and added to the bit-vector constraint. Note that these constraints leave the middle 4 bits of B unconstrained.

— HAMPI encodes the union operator $(+)$ as a disjunction in the bit-vector logic. This results in 6 disjuncts for the above formula, where each disjunct is an equality constraint. For example, the formula corresponding to the first regular expression ()()()

function RegexpToBV(Bitvector B variable of appropriate length, regular rexpression *RegExp*)
output: bitvector assertions
switch *RegExp* **do**

    case *C* //string-constant

        Let C_{bv} be the bit-vector representation of C

        $\bigwedge_{i=0}^{i=len(C)} B[i] = C_{bv}[i]$

    case $R_1 + R_2$ //union

        RegexpToBV(B, R_1) $\vee$ RegexpToBV(B, R_2)

    case $R_1 R_2$ //concatenation

        L = Length(*RegExp*)

        $\bigvee_{len(R_1)=1}^{len(R_1)=L}$ (RegexpToBV($B[0 : len(R_1) − 1], R_1$) $\wedge$ RegexpToBV($B[len(R_1) : len(R_1) + len(R_2)], R_2$))

    case *Bounded KleeneStar($R_1, R_2, \ldots, R_n$)*

        $\bigvee_{\{\text{All partition lengths over } R_1, \ldots, R_n\}}$ (RegexpToBV($B[0 : len(R_1) − 1], R_1$) $\wedge \ldots \wedge$

        RegexpToBV($B[len(R_{n−1}) : len(R_1) + \ldots + len(R_n)], R_n$))

endsw

Fig. 7. Pseudo code for translating HAMPI string constraints into bit-vector constraints. For a string constraint $StrExp \in RegExp$, HAMPI creates a bitvector B of length($StrExp$), and calls RegexpToBV(B, *RegExp*) to create constraints.

is as follows.

$$B[0 : 0] = 0 \wedge B[1 : 1] = 1 \wedge \ldots \wedge B[5 : 1] = 1$$

—HAMPI encodes the concatenation operator by enumerating all possible distributions of the characters to the subexpressions, encoding the subexpressions recursively, and combining the sub-formulas in a disjunction.

After STP finds a solution to the bit-vector formula (if one exists), HAMPI decodes the solution by reading 8-bit subvectors as consecutive ASCII characters.

3.4. Complexity

The satisfiability problem for HAMPI's logic (core form string constraints) is NP-complete.

To show NP-hardness, we reduce the 3-CNF (conjunctive normal form) Boolean satisfiability problem to the satisfiability problem of the core form string constraints in HAMPI's logic. Consider an arbitrary 3-CNF formula with n Boolean variables and m clauses. A clause in 3-CNF is a disjunction ($\vee$) of three literals. A literal is a Boolean variable (v_i) or its negation ($\neg v_i$). For every 3-CNF clause, a HAMPI constraint can be generated. Let $\Sigma = \{$T, F$\}$ denote the alphabet. For the clause ($v_0 \vee v_1 \vee \neg v_2$), the equivalent HAMPI constraint is:

$$V \in (\text{T}\Sigma\Sigma \cdots \Sigma \ + \ \Sigma\text{T}\Sigma \cdots \Sigma \ + \ \Sigma\Sigma\text{F} \cdots \Sigma),$$

where the HAMPI variable V is an n-character string representing the possible assignments to all n Boolean variables satisfying the input 3-CNF formula. Each of the HAMPI regular-expression disjuncts in the core form string constraint shown above, such as $\text{T}\Sigma\Sigma \cdots \Sigma$, contains n conjuncts and has a T in the ith slot for v_i (and F for $\neg v_i$), that is,

$$v_i \longrightarrow \underbrace{\overbrace{\Sigma \cdots \Sigma}^{i-1} \text{T} \overbrace{\Sigma \cdots \Sigma}^{n-i}}_{n}.$$

The total number of such HAMPI constraints is m, the number of clauses in the input 3-CNF formula (here $m = 1$). This reduction from a 3-CNF Boolean formula into HAMPI is clearly polynomial-time.

To establish that the satisfiability problem for HAMPI's logic is in NP, we only need to show that for any set of core form string constraints, there exists a polynomial-time verifier that can check any short witness. The size of a set of core form string constraints is the size k of the string variable plus the sum r of the sizes of regular expressions. A witness has to be of size k, and it is easy to check, in time polynomial in $k+r$, whether the witness belongs to each regular language.

3.5. Example of Constraint Solving

We now illustrate the entire constraint solving process end-to-end on a simple example. Given the following input.

```
var v:2..2; // fixed-size string of length 2
cfg E := "()" | E E | "(" E ")";
reg Efixed := fixsize(E, 6);
val q := concat( "((" , v , "))" );
assert q in Efixed;     // turns into constraint c1
assert q contains "())"; // turns into constraint c2
```

HAMPI tries to find a satisfying assignment for variable v by following the four-step algorithm[2] in Figure 3.

Step 1. Normalize constraints to core form, using the algorithm in Section 3.2:

$$\textbf{c1}\;[\texttt{assert q in Efixed}]: \qquad ((\,v\,)) \quad \in \quad ()\big[()() + (())\big] + \\ \big[()() + (())\big]() + \\ (\big[()() + (())\big])$$

$$\textbf{c2}\;[\texttt{assert q contains "())"}]: \quad ((\,v\,)) \quad \in \quad \big[(\,+\,)\big]\star\,()\,\big[(\,+\,)\big]\star$$

Step 2. Encode the core-form constraints in bit-vector logic. We show how HAMPI encodes constraint **c1**; the process for **c2** is similar. HAMPI creates a bit-vector variable bv of length 6*8=48 bits, to represent the left-hand side of **c1** (since Efixed is 6 bytes). Characters are encoded using ASCII codes: '(' is 40 in ASCII, and ')' is 41. HAMPI encodes the left-hand-side expression of **c1**, $((\,v\,))$, as formula L_1, by specifying the constant values:

$$L_1 : (bv[0] = 40) \wedge (bv[1] = 40) \wedge (bv[4] = 41) \wedge (bv[5] = 41).$$

Bytes $bv[2]$ and $bv[3]$ are reserved for v, a 2-byte variable. The top-level regular expression in the right-hand side of **c1** is a 3-way union, so the result of the encoding is a 3-way disjunction. For the first disjunct $()\big[()() + (())\big]$, HAMPI creates the following formula D_{1a}:

$$bv[0] = 40 \wedge bv[1] = 41 \wedge$$

$$\big((bv[2] = 40 \wedge bv[3] = 41 \wedge bv[4] = 40 \wedge bv[5] = 41)\vee$$

$$\big(bv[2] = 40 \wedge bv[3] = 40 \wedge bv[4] = 41 \wedge bv[5] = 41\big)\big).$$

Formulas D_{1b} and D_{1c} for the remaining conjuncts are similar. The bit-vector formula that encodes **c1** is

$$C_1 = L_1 \wedge \big(D_{1a} \vee D_{1b} \vee D_{1c}\big).$$

---

[2]The alphabet of the regular expression or context-free grammar in a HAMPI input is implicitly restricted to the terminals specified.

Similarly, a formula C_2 (not shown here) encodes **c2**. The formula that HAMPI sends to the STP solver is

$$(C_1 \wedge C_2).$$

Step 3. STP finds a solution that satisfies the formula:

$$bv[0] = 40, bv[1] = 40, bv[2] = 41, bv[3] = 40, bv[4] = 41, bv[5] = 41.$$

In decoded ASCII, the solution is "(()())" (quote marks not part of solution string).

Step 4. HAMPI reads the assignment for variable v off of the STP solution, by decoding the elements of bv that correspond to v, that is, elements 2 and 3. HAMPI reports the solution for v as ")(".

String "()" is another legal solution for v, but STP only finds one solution.

4. OPTIMIZATIONS

We now describe some optimizations we implemented in HAMPI to reduce running time.

4.1. Memoization

HAMPI stores and reuses partial results during the computation of fixed-sizing of context-free grammars (Section 3.2) and during the encoding of core constraints in bit-vector logic (Section 3.3).

To illustrate, consider the example from Section 3.5, that is, fixed-sizing the context-free grammar of well-balanced parentheses to size 6.

```
cfg E := "()" | E E | "(" E ")" ;
```

Consider the second production E := E E. There are two ways to construct a string of 6 characters: Either construct 2 characters from the first occurrence of E and construct 4 characters from the second occurrence, or vice-versa. After creating the regular expression that corresponds to the first of these ways, HAMPI creates the second expression from the memoized subresults. HAMPI's implementation shares the memory representations of common subexpressions. For example, HAMPI uses only one object to represent all three occurrences of ()() + (()) in constraint **c1** of the example in Section 3.5.

4.2. Constraint Templates

Constraint templates capture common encoded subexpressions, modulo offset in the bit-vector. During the bit-vector encoding step (Section 3.3), HAMPI may encode the same regular expression multiple times as bit-vector formulas, as long as the underlying offsets in the bit-vector are different. For example, the (constant) regular expression ")(" may be encoded as $(bv[0] = 41) \wedge (bv[1] = 40)$ or as $(bv[3] = 41) \wedge (bv[4] = 40)$, depending on the offset in the bit-vector (0 and 3, respectively)[3].

HAMPI creates a single "template", parameterized by the offset, for the encoded expression, and instantiates the template every time, with appropriate offsets. For the example above, the template is $T(p) \equiv bv[p] = 41 \wedge bv[p+1] = 40$, where p is the offset parameter. HAMPI then instantiates the template to $T(0)$ and $T(3)$.

As another example, consider **c1** in Section 3.5: The subexpression ()()+(()) occurs 3 times in **c1**, each time with a different offset (2 for the first occurrence, 0 for the second, and 1 for the third). The constraint-template optimization enables HAMPI to do the encoding once and reuse the results, with appropriate offsets.

---

[3]40 is the ASCII code for the (character, and 41 is the code for).

4.3. Server Mode

Server mode improves HAMPI's efficiency on simple constraints and repeated calls. Because HAMPI is a Java program, the startup time of the Java virtual machine may be a significant overhead when solving small constraints. Therefore, we added a server mode to HAMPI, in which the (constantly running) solver accepts inputs passed over a network socket and returns results over the same socket. This enables HAMPI to be efficient over repeated calls, for tasks like solving the same constraints on string variables of different sizes.

5. EVALUATION

We experimentally tested HAMPI's applicability to practical problems involving string constraints and compared HAMPI's performance and scalability to another string-constraint solver. We ran the following four experiments.

(1) We used HAMPI in a static-analysis tool [Wassermann and Su 2007] that identifies possible SQL injection vulnerabilities (Section 5.1).
(2) We used HAMPI in Ardilla [Kiezun et al. 2009b], a dynamic-analysis tool that creates SQL injection attacks (Section 5.2).
(3) We used HAMPI in Klee, a systematic testing tool for C programs (Section 5.3).
(4) We compared HAMPI's performance and scalability to CFGAnalyzer [Axelsson et al. 2008], a solver for bounded versions of context-free-language problems, for instance, intersection (Section 5.4).

Unless otherwise noted, we ran all experiments on a 2.2GHz Pentium 4 PC with 1 GB of RAM running Debian Linux, executing HAMPI on Sun Java Client VM 1.6.0-b105 with 700MB of heap space. We ran HAMPI with all optimizations on, but flushed the whole internal state after solving each input to ensure fairness in timing measurements, that is, preventing artificially low runtimes when solving a series of structurally-similar inputs.

The results of our experiments demonstrate that HAMPI is expressive in encoding real constraint problems that arise in security analysis and automated testing, that it can be integrated into existing testing tools, and that it can efficiently solve large constraints obtained from real programs.

HAMPI's source code and documentation, experimental data, and additional results are available at `http://people.csail.mit.edu/akiezun/hampi`.

5.1. Identifying SQL Injection Vulnerabilities Using Static Analysis

We evaluated HAMPI's applicability to finding SQL injection vulnerabilities in the context of a static analysis. We used the tool from Wassermann and Su [2007] that, given source code of a PHP Web application, identifies potential SQL injection vulnerabilities. The tool computes a context-free grammar G that conservatively approximates all string values that can flow into each program variable. Then, for each variable that represents a database query, the tool checks whether $L(G) \cap L(R)$ is empty, where $L(R)$ is a regular language that describes undesirable strings or attack vectors (strings that can exploit a security vulnerability). If the intersection is empty, then Wassermann and Su's tool reports the program to be safe. Otherwise, the program may be vulnerable to SQL injection attacks.

An example $L(R)$ that Wassermann and Su use—the language of strings that contain an odd number of unescaped single quotes—is given by the regular expression (we used this R in our experiments):

$$R = \begin{array}{l} \texttt{(([^']|\\')*[^\\])?'} \\ \texttt{((([^']|\\')*[^\\])?'} \\ \texttt{(([^']|\\')*[^\\])?'([^']|\\')*} \end{array}$$

Using HAMPI in such an analysis offers two important advantages. First, it eliminates a time-consuming and error-prone reimplementation of a critical component: the string-constraint solver. To compute the language intersection, Wassermann and Su implemented a custom solver based on the algorithm by Minamide [2005]. Second, HAMPI creates concrete example strings from the language intersection, which is important for generating attack vectors; Wassermann and Su's custom solver only checks for emptiness of the intersection, and does not create example strings.

Using a fixed-size string-constraint solver, such as HAMPI, has its limitations. An advantage of using an unbounded-length string-constraint solver is that if the solver determines that the input constraints have no solution, then there is indeed no solution. In the case of HAMPI, however, we can only conclude that there is no solution of the given size.

Experiment. We performed the experiment on 6 PHP applications. Of these, 5 were applications used by Wassermann and Su to evaluate their tool [Wassermann and Su 2007]. We added 1 large application (`claroline`, a builder for online education courses, with 169 kLOC) from another paper by the same authors [Wassermann and Su 2008]. Each of the applications has known SQL injection vulnerabilities. The total size of the applications was 339,750 lines of code.

Wassermann and Su's tool found 1,367 opportunities to compute language intersection, each time with a different grammar G (built from the static analysis) but with the same regular expression R describing undesirable strings. For each input (i.e., pair of G and R), we used both HAMPI and Wassermann and Su's custom solver to compute whether the intersection $L(G) \cap L(R)$ was empty.

When the intersection is *not* empty, Wassermann and Su's tool cannot produce an example string for those inputs, but HAMPI can. To do so, we varied the size N of the string variable between 1 and 15, and for each N, we measured the total HAMPI solving time, and whether the result was UNSAT or a satisfying assignment.

Results. We found empirically that when a solution exists, it can be very short. In 306 of the 1,367 inputs, the intersection was not empty (both solvers produced identical results). Out of the 306 inputs with nonempty intersections, we measured the percentage for which HAMPI found a solution (for increasing values of N): 2% for $N = 1$, 70% for $N = 2$, 88% for $N = 3$, and 100% for $N = 4$. That is, in this large dataset, all nonempty intersections contain strings with no longer than 4 characters.

Due to false positives inherent in Wassermann and Su's static analysis, the strings generated from the intersection do not necessarily constitute real attack vectors. However, this is a limitation of the static analysis, not of HAMPI.

We measured how HAMPI's solving time depends on the size of the grammar. We measured the size of the grammar as the sum of lengths of all productions (we counted ϵ-productions as of length 1). Among the 1,367 grammars in the dataset, the mean size was 5490.5, standard deviation 4313.3, minimum 44, maximum 37955. We ran HAMPI for $N = 4$, that is, the length at which all satisfying assignments were found. Figure 8 shows the solving time as a function of the grammar size, for all 1,367 inputs.

HAMPI can solve most queries quickly. Figure 9 shows the percentage of inputs that HAMPI can solve in the given time, for $1 \leq N \leq 4$, that is, until all satisfying assignments are found. For $N = 4$, HAMPI can solve 99.7% of inputs within 1 second. There were 5 queries for which HAMPI spent more than 130 seconds on each. We examined these inputs and concluded that the unusually long solving time was due to the very large size of the grammar (more than 37000 productions in each input).

Summary of results. We applied HAMPI to 1,367 constraints created from analysis of 339,750 lines of code from 6 PHP applications. HAMPI found that all 306 satisfiable
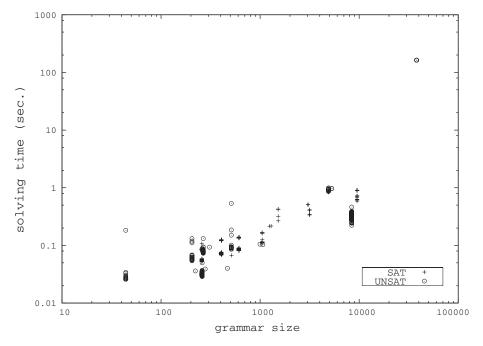
Fig. 8. HAMPI solving time as function of grammar size (number of all elements in all productions), on 1,367 inputs from the Wassermann and Su [Wassermann and Su 2007] dataset. The size of the string variable was 4, the smallest at which HAMPI finds all satisfying assignments for the dataset. Each point represents an input; shapes indicate SAT/UNSAT. Section 5.1 describes the experiment.

constraints have short solutions ($N \leq 4$). HAMPI found all known solutions, and solved 99.7% of the generated constraints in less than 1 second per constraint. These results, obtained on a large dataset from a powerful static analysis and real Web applications, show that HAMPI's fixed-size solving algorithm is applicable to real problems.

5.2. Creating SQL Injection Attacks Using Dynamic Analysis

We evaluated HAMPI's ability to automatically find SQL injection attack strings using constraints produced by running a dynamic-analysis tool on PHP Web applications. For this experiment, we used Ardilla [Kiezun et al. 2009b], a tool that constructs SQL injection and Cross-site Scripting (XSS) attacks by combining automated input generation, dynamic tainting, and generation and evaluation of candidate attack strings.

One component of Ardilla, the *attack generator*, creates candidate attack strings from a pre-defined list of attack patterns. Though its pattern list is extensible, Ardilla's attack generator is neither targeted nor exhaustive: The generator does not attempt to create valid SQL statements but rather simply assigns predefined values from the attack patterns list one-by-one to variables identified as vulnerable by the dynamic tainting component; it does so until an attack is found or until there are no more patterns to try.

For this experiment, we replaced the attack generator with the HAMPI string solver. This reduces the problem of finding SQL injection attacks to one of string constraint generation followed by string constraint solving. This replacement makes attack creation targeted and exhaustive: HAMPI constraints encode the SQL grammar and, if there is an attack of a given length, HAMPI is sure to find it.

To use HAMPI with Ardilla, we also replaced Ardilla's dynamic tainting component with a concolic execution [Godefroid et al. 2005; Sen et al. 2005] component. This
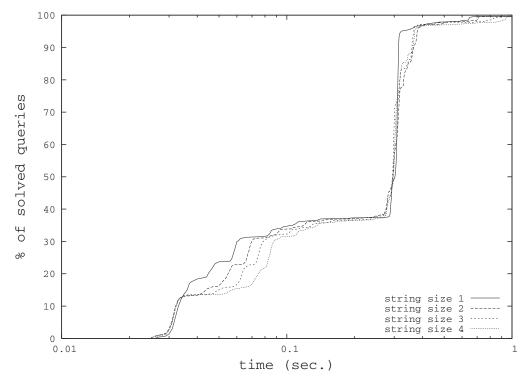
Fig. 9. Percentage of queries solvable by HAMPI, in a given amount of time, on data from Wassermann and Su [2007]. Each line represents a distribution for a different size of the string variable. All lines reach 99.7% at 1 second and 100% before 160 seconds. Section 5.1 describes the experiment.

required code changes that were quite extensive but fairly standard. Concolic execution creates and maintains symbolic expressions for each concrete runtime value derived from the input. For example, if a value is derived as a concatenation of user-provided parameter p and a constant string "abc," then its symbolic expression is concat(p, "abc"). This component is required to generate the constraints for input to HAMPI.

The HAMPI input includes a partial SQL grammar (similar to that in Figure 2). We wrote a grammar that covers a subset of SQL queries commonly observed in Web applications, which includes SELECT, INSERT, UPDATE, and DELETE, all with WHERE clauses. The grammar size is 74, according to the metric of Section 5.1. Each terminal is represented by a single unique character.

We ran our modified Ardilla on 5 PHP applications (the same set as the original Ardilla study [Kiezun et al. 2009b], totaling 14,941 lines of PHP code). The original study identified 23 SQL injection vulnerabilities in these applications. Ardilla generated 216 HAMPI inputs, each of which is a string constraint built from the execution of a particular path through an application. For each constraint, we used HAMPI to find an attack string of size $N \leq 6$—a solution corresponds to the value of a vulnerable PHP input parameter. Following previous work [Fu et al. 2007; Halfond et al. 2008], the generated constraint defined an attack as a syntactically valid (according to the grammar) SQL statement with a tautology in the WHERE clause, for instance, OR 1=1. We used 4 tautology patterns, distilled from several security lists.[4]

---

[4] http://www.justinshattuck.com/2007/01/18/mysql-injection-cheat-sheets.,
http://ferruh.mavituna.com/sql-injection-cheatsheet-oku,
http://pentestmonkey.net/blog/mysql-sql-injection-cheat-sheet

We separately measured solving time for each tautology and each choice of *N*. A security-testing tool like Ardilla might search for the shortest attack string for *any* of the specified tautologies.

Summary of results. HAMPI fully replaced Ardilla's custom attack generator. HAMPI successfully created all 23 attacks on the tested applications. HAMPI solved the associated constraints quickly, finding all known solutions for $N \leq 6$. HAMPI solved 46.0% of those constraints in less than 1 second per constraint, and solved all the constraints in less than 10 seconds per constraint.

These results show that the HAMPI enabled a successful reduction of the problem of finding SQL injection attacks to string constraint generation and solving, and was able to plug into an existing security testing application and perform comparably.

5.3. Systematic Testing of C Programs

We combined HAMPI with a state-of-the-art systematic testing tool, Klee [Cadar et al. 2008], to improve Klee's ability to create valid test cases for programs that accept highly structured string inputs.

Automatic test-case generation tools that use combined concrete and symbolic execution, also known as *concolic execution* [Sen et al. 2005; Godefroid et al. 2005; Cadar et al. 2006; Cadar et al. 2008; Godefroid et al. 2008b; Jayaraman et al. 2009] have trouble creating test cases that achieve high coverage for programs that expect structured inputs, such as those that require input strings from a context-free grammar [Majumdar and Xu 2007; Godefroid et al. 2008a]. The parser components of programs that accept structured inputs (especially those auto-generated by tools such as Yacc) often contain complex control-flow with many error paths; the vast majority of paths that automatic testers explore terminate in parse errors, thus creating inputs that do not lead the program past the initial parsing stage.

Testing tools based on concolic execution mark the target program's input string as totally unconstrained (i.e., *symbolic*) and then build up constraints on the input based on the conditions of branches taken during execution. If there were a way to constrain the symbolic input string so that it conforms to a target program's specification (e.g., a context-free grammar), then the testing tool would only explore nonerror paths in the program's parsing stage, thus resulting in generated inputs that reach the program's core functionality.

To demonstrate the feasibility of this technique, we used HAMPI to create grammar-based input constraints and then fed those into Klee [Cadar et al. 2008] to generate test cases for C programs. We compared the coverage achieved and numbers of legal (and rejected) inputs generated by running Klee with and without the HAMPI constraints.

Similar experiments have been performed by others [Majumdar and Xu 2007; Godefroid et al. 2008a], and we do not claim novelty for the experimental design. However, previous studies used custom-made string solvers, while we applied HAMPI as an "off-the-shelf" solver without modifying Klee.

Klee provides an API for target programs to mark inputs as symbolic and to place constraints on them. The code snippet below uses klee_assert to impose the constraint that all elements of buf must be numeric before the target program runs.

```
char buf[10]; // program input
klee_make_symbolic(buf, 10); // make all 10 bytes symbolic
```

```
// constrain buf to contain only decimal digits
for (int i = 0; i < 10; i++)
  klee_assert(('0' <= buf[i]) && (buf[i] <= '9'));

run_target_program(buf); // run target program with buf as input
```

HAMPI simplifies writing input-format constraints. Simple constraints, such as those above, can be written by hand, but it is infeasible to manually write more complex constraints for specifying, for example, that buf must belong to a particular context-free language. We use HAMPI to automatically compile such constraints from a grammar down to C code, which can then be fed into Klee.

We chose 3 open-source programs that specify expected inputs using context-free grammars in Yacc format (a subset of those used by Majumdar and Xu [2007]). cueconvert converts music playlists from .cue format to .toc format. logictree is a solver for propositional logic formulas. bc is a command-line calculator and simple programming language. All programs take input from stdin; Klee allows the user to create a fixed-size symbolic buffer to simulate stdin, so we did not need to modify these programs.

For each target program, we ran the following experiment on a 3.2GHz Pentium 4 PC with 1GB of RAM running Fedora Linux.

(1) Automatically convert its Yacc specification into HAMPI's input format (described in Section 3.1), using a script we wrote. To simplify lexical analysis, we used either a single letter or numeric digit to represent certain tokens, depending on its Lex specification (this should not reduce coverage in the parser).

(2) Add a fixed-size restriction to limit the input to N bytes. Klee (similar to, for example, SAGE [Godefroid et al. 2008b]) actually requires a fixed-size input, which matches well with HAMPI's fixed-size input language. We empirically picked N as the largest input size for which Klee does not run out of memory. We augmented the HAMPI input to allow for strings with arbitrary numbers of trailing spaces, so that we can generate program inputs *up to* size N.

(3) Run HAMPI to compile the input grammar file into STP bit-vector constraints (described in Section 3.3).

(4) Automatically convert the STP constraints into C code that expresses the equivalent constraints using C variables and calls to klee_assert(), with a script we wrote (the script performs only simple syntactic transformations since STP operators map directly to C operators).

(5) Run Klee on the target program using an N-byte input buffer, first marking that buffer as symbolic, then executing the C code that imposes the input constraints, and finally executing the program itself.

(6) After a 1-hour time-limit expires, collect all generated inputs and run them through the original program (compiled using gcov) to measure coverage and legality of each input.

(7) As a control, run Klee for 1 hour using an N-byte symbolic input buffer (with no initial constraints), collect test cases, and run them through the original program to measure coverage and legality of each input.

Table I summarizes our experimental setup and results. We made 3 sets of measurements: total line coverage, line coverage in the Yacc parser file that specifies the grammar rules alongside C code snippets denoting parsing actions, and numbers of inputs (test cases) generated, as well as how many of those inputs were *legal* (i.e., not rejected by the program as a parse error).

The result of using HAMPI grammars to improve coverage of test cases generated by the Klee systematic testing tool. ELOC lists *Executable* Lines of Code, as counted by `gcov` over all `.c` files in program (whole-project line counts are several times larger, but much of that code does not directly execute). Each trial was run for 1 hour. To create minimal test suites, Klee only generates a new input when it covers new lines that previous inputs have not yet covered; the total number of explored paths is usually 2 orders of magnitude greater than the number of generated inputs. Column symbolic shows results for runs of Klee without a HAMPI grammar. Column symbolic + grammar shows results for runs of Klee with a HAMPI grammar. Column combined shows accumulated results for both kinds of runs. Section 5.3 describes the experiment.

cueconvert (939 ELOC, 28-byte input)	symbolic	symbolic + grammar	combined
% total line coverage:	32.2%	51.4%	56.2%
% parser file line coverage (48 lines):	20.8%	77.1%	79.2%
# legal inputs / # generated inputs (%):	0 / 14 (0%)	146 / 146 (100%)	146 / 160 (91%)

logictree (1,492 ELOC, 7-byte input)	symbolic	symbolic + grammar	combined
% total line coverage:	31.2%	63.3%	66.8%
% parser file line coverage (17 lines):	11.8%	64.7%	64.7%
# legal inputs / # generated inputs (%):	70 / 110 (64%)	98 / 98 (100%)	168 / 208 (81%)

bc (1,669 ELOC, 6-byte input)	symbolic	symbolic + grammar	combined
% total line coverage:	27.1%	43.0%	47.0%
% parser file line coverage (332 lines):	11.8%	39.5%	43.1%
# legal inputs / # generated inputs (%):	2 / 27 (5%)	198 / 198 (100%)	200 / 225 (89%)

The run times for converting each Yacc grammar into HAMPI format, fixed-sizing to N bytes, running HAMPI on the fixed-size grammar, and converting the resulting STP constraints into C code are negligible; together, they took less than 1 second for each of the 3 programs.

Using HAMPI in Klee improved coverage. Constraining the inputs using a HAMPI grammar resulted in up to $2\times$ improvement in total line coverage and up to $5\times$ improvement in line coverage within the Yacc parser file. Also, as expected, it eliminated all illegal inputs.

Using both sets of inputs (combined column) improved upon the coverage achieved using the grammar by up to 9%. Upon manual inspection of the extra lines covered, we found that it was due to the fact that the runs with and without the grammar covered nonoverlapping sets of lines: The inputs generated by runs without the grammar (symbolic column) covered lines dealing with processing parse errors, whereas the inputs generated with the grammar (symbolic + grammar column) never had parse errors and covered core program logic. Thus, combining test suites is useful for testing both error and regular execution paths.

With HAMPI's help, Klee uncovered more errors. Using the grammar, Klee generated 3 distinct inputs for logictree that uncovered (previously unknown) errors where the program entered an infinite loop. We do not know how many distinct errors these inputs identify.

Without the grammar, Klee was not able to generate those same inputs within the 1-hour time limit; given the structured nature of those inputs (e.g., one is "@x $y z"), it is unlikely that Klee would be able to generate them within any reasonable time bound without a grammar.

We manually inspected lines of code that were not covered by any strategy. We discovered two main hindrances to achieving higher coverage: First, the input sizes were still too small to generate longer productions that exercised more code, especially problematic for the playlist files for cueconvert; this is a limitation of Klee running out of memory and not of HAMPI. Second, while grammars eliminated all parse errors, many generated inputs still contained semantic errors, such as malformed bc expressions and function definitions (again, unrelated to HAMPI).

Summary of results. Using HAMPI to create input constraints led to up to $2\times$ improvements in line coverage (up to $5\times$ coverage improvements in parser code), eliminated all illegal inputs, and enabled discovering 3 distinct, previously unknown, inputs that led to infinitely-looping program execution.

These results show that using HAMPI can improve the effectiveness of automated test-case generation and bug finding tools.

5.4. Comparing Performance to CFGAnalyzer

We evaluated HAMPI's utility in analyzing context-free grammars, and compared HAMPI's performance to a specialized decision procedure, CFGAnalyzer [Axelsson et al. 2008]. CFGAnalyzer is a SAT-based decision procedure for bounded versions of 6 problems (5 undecidable) that involve context-free grammars: universality, inclusion, intersection, equivalence, ambiguity, and emptiness (decidable). We downloaded the latest available version[5] (released 3 December 2007) and configured the program according to the manual.

Experiment. We performed the CFGAnalyzer experiments with the grammar-intersection problem. Five of six problems handled by CFGAnalyzer (universality, inclusion, intersection, equivalence, and emptiness) can be easily encoded as HAMPI inputs; the intersection problem is representative of the rest.

In the experiments, both HAMPI and CFGAnalyzer searched for strings (of fixed length) from the intersection of 2 grammars. To avoid bias, we used CFGAnalyzer's own experimental data sets (obtained from the authors). From the set of 2088 grammars in the data set, we selected a random sample of 100 grammar pairs. We used both HAMPI and CFGAnalyzer to search for strings of lengths $1 \leq N \leq 50$. We ran CFGAnalyzer in a nonincremental mode (in the incremental mode, CFGAnalyzer reuses previously computed subsolutions), to create a fair comparison with HAMPI, which ran as usual in server mode while flushing its entire internal state after solving each input. We ran both programs without a timeout.

Figure 10 shows the results averaged over all pairs of grammars. HAMPI is faster than CFGAnalyzer for all sizes larger than 4 characters. Importantly, HAMPI's win over CFGAnalyzer grows as the size of the problem increases (up to $6.8\times$ at size 50). For the largest problems ($N = 50$), HAMPI was faster (by up to $3000\times$) on 99 of the 100 grammar pairs, and $1.3\times$ slower on the remaining 1 pair of grammars (data available on HAMPI Web site).

HAMPI is faster also on grammar-membership constraints. We performed an additional experiment: searching for any string of a given length from a context-free grammar. The results were similar to those for intersection: for instance, HAMPI finds a string of size 50, on average, in 1.5 seconds, while CFGAnalyzer finds one in 8.7 seconds ($5.8\times$ difference). The HAMPI website contains the experimental data and results.

Summary of results. On average, HAMPI solved constraints up to $6.8\times$ faster than CFGAnalyzer, and its lead increased as the problem size grew larger.

6. RELATED WORK

Decision procedures have received widespread attention within the context of program analysis, testing, and verification. Decision procedures exist for theories such as Boolean satisfiability [Moskewicz et al. 2001], bit-vectors [Ganesh and Dill 2007], quantified Boolean formulas [Biere 2005], and linear arithmetic [de Moura and Bjørner 2008]. In contrast, there has been relatively little work on practical and expressive solvers that reason about strings or sets of strings directly.

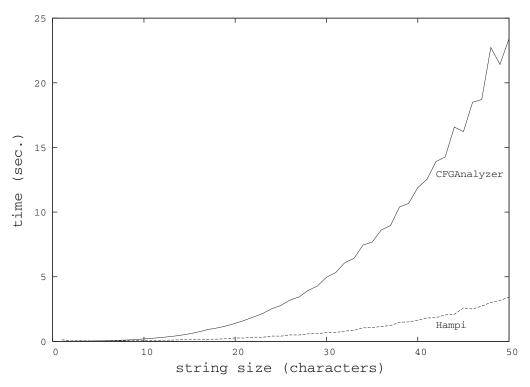[5]http://www.tcs.ifi.lmu.de/~mlange/cfganalyzer.

Fig. 10. Solving time as a function of string size, on context-free-grammar intersection constraints. Results are averaged over 100 randomly-selected pairs of context-free grammars. Section 5.4 describes the experiment.

6.1. Practical Solvers for String Constraints

MONA [Klarlund 1998] uses finite-state automata and tree automata to reason about sets of strings. However, the user still has to translate their input problem into MONA's input language (weak monadic second-order theory of one successor). MONA also provides automata-based tools, similar to other libraries [AT&T FSM Library 1997; van Noord 2010; Møller 2010].

Word equations [Rajasekar 1994; Bjørner et al. 2009] describe equality between two strings that contain string variables. Rajasekar [1994] proposes a logic programming approach that includes constraints on individual words. His solver handles concatenation but not regular language membership. Bjørner et al. [2009] describe a constraint solver for word queries over a variety of operations, and translate string constraints to the language of the Z3 solver [de Moura and Bjørner 2008]. If there is a solution, Z3 returns a finite bound for the set of strings, that is then explored symbolically. String solvers SUSHI [Fu and Li 2010] and STRANGER [Yu et al. 2010a] focus on modeling string replacement. Multiple string solvers are based on automata, for example [Veanes et al. 2010; Yu et al. 2010b]. Hooimeijer and Veanes [2011] present a comparison of a few automata-based solvers. The procedure described by Yu et al. [2009] combines string and length constraints, which enables verification of properties that are beyond the capability of string solvers, such as HAMPI, that do not model length constraints. Kaluza [2010], a string solver built on top of HAMPI and STP and embedded in the Kuzdu JavaScript bugfinding tool [Saxena et al. 2010], reuses HAMPI's encoding regular-language constraints into bitvectors. Kaluza supports multiple string

variables, concatenation function, equations over string terms, length function over string terms and regular expressions. Unlike HAMPI, these tools do not support context-free grammars directly.

Hooimeijer and Weimer [2009] describe a decision procedure for regular-language constraints, focusing on generating sets of satisfying assignments rather than individual strings. Unlike HAMPI, their solver does not allow expressing fixed-size context-free grammars.

Hooimeijer and Veanes [2011] conducted a performance comparison of several different automata algorithms and datastructures within the context of string constraint solving. They found that a BDD-based character set representation is most performant for alphabets. This work supplements previous work by Veanes et al. [2010] on symbolic automata, and work by Hooimeijer and Weimer [2010] on lazy search algorithms. The work by Veanes et al. focuses on a first-order encoding of automata directly into an SMT solver. HAMPI similarly encodes directly to a constraint solver, but without the use of quantifiers and without an intermediate automaton representation. Consequently, many of the performance optimizations for automata-based techniques do not apply to HAMPI. However, some of the results in this related work indicate that it may be interesting to attempt HAMPI's automaton-less translation in a setting that supports quantifiers.

Yu et al. [2010b] focus on the integration of string constraints with length constraints, as well as the relational analysis of string constraints. The approaches of Yu et al. [2009] and Yu et al. [2010b] are based on multitrack automata or transducers. The work on relational analysis includes an undecidability result, and the algorithmic contribution is a sound over approximation. In contrast, HAMPI is based on a decidable core theory that can be solved without approximation. Relational analysis is most useful in the context of programs rather than constraint systems, and, indeed, the language presented by Yu et al. [2010b] includes features like goto and assignment. We instead focus on a pure constraint language that permits a variety of distinct frontend constraint generators, as outlined in our experiments (Section 5).

Finally, a few recent approaches include support for operations such as substring extraction with nontrivial integer bounds. Kaluza [2010] uses an external solver for integer constraints. Internally, Kaluza eliminates high-level operations (e.g., `substring` and `indexOf`) using a combination of low-level constraints on string lengths (using an external solver) and string contents (using HAMPI). Bjørner et al. [2009] perform a translation that is similar in spirit, but rely on a single solver for constraints on both length and content. Since HAMPI's underlying STP solver supports the required operations, it is feasible to extend our approach to support positional constraints in an analogous way.

6.2. String Solvers Built as Part of Program Analysis Applications

Many analyses use custom solvers for string constraints [Godefroid et al. 2008a; Christensen et al. 2003; Minamide 2005; Wassermann and Su 2007, 2008; Wassermann et al. 2008; Emmi et al. 2007; Fu et al. 2007]. All of these approaches include some implementation for language intersection and language inclusion; most, similarly to HAMPI, can perform regular-language intersection. Each of these implementations is tightly integrated with the associated program analysis, making a direct comparison with HAMPI impractical.

Christensen et al. [2003] have a static analysis tool to check for SQL injection vulnerabilities that uses automata-based techniques to represent over-approximation of string values. Fu et al. [2007] also use an automata-based method to solve string constraints. Ruan et al. [2008] use a first-order encoding of string functions occurring in C programs, and solve the constraints using a linear arithmetic solver.

Besides the custom solvers by Wassermann and Su [2007], the solver by Emmi et al. [2007] is closest to HAMPI. Emmi et al. used their solver for automatic test case generation for database applications. Unlike HAMPI, their solver allows constraints over unbounded regular languages and linear arithmetic, but does not support context-free grammars.

Many of the program analyses listed here perform similar tasks when reasoning about string-valued variables. This is strong evidence that a unified approach, in the form of an external string-constraint solvers such as HAMPI, is warranted.

6.3. Theoretical Work on String Constraints

A variety of problems involve strings constraints, and there is an extensive literature on the theoretical study of these problems [Makanin 1977; Pesant 2004; Quimper and Walsh 2006].

In his original paper, Quine [1946] showed that the first-order theory of string equations (i.e., quantified sentences over Boolean combination of word equations) is undecidable. Many sub-theories and extensions have been studied since.

One line of research studies fragments and modifications of this base theory which are decidable. Makanin [1977] famously proved that the satisfiability problem for the quantifier-free theory of word equations is decidable. Plandowski [2006] and co-authors showed that the complexity of this problem is in PSPACE.

Schulz [1992] extended Makanin's satisfiability algorithm to the class of formulas where each variable in the equations is specified to lie in a given regular set. This is a strict generalization of the solution sets of word equations. Karhumäki et al. [2000] shows that the class of sets expressible through word equations is incomparable to that of regular sets.

Word equations augmented with additional predicates yield richer structures which are relevant to many applications. In the 1970s, Matiyasevich formulated a connection between string equations augmented with integer coefficients whose integers are taken from the Fibonacci sequence and Diophantine equations [Matiyasevich 2008]. In particular, he showed that proving undecidability for the satisfiability problem of the theory of word equations and length constraints would suffice to solve Hilbert's 10th Problem in a novel way. The problem remains open. Another related problem, namely, the decidability of the satisfiability problem for the quantifier-free theory of word equations, length constraints and membership predicate over regular expressions is also open.

Recently, the first decidability results regarding the above-mentioned open problems were proved [Ganesh et al. 2011], under a certain minimal and practical condition. In particular, the authors proved that if word equations can be converted into a solved form [Barrett 2003], a concept well known in automated reasoning and SMT solver community, then the satisfiability problem for word equations and length constraints is decidable. Ganesh et al. [2011] further show that if the solved form of the given word equations are regular expressions then the quantifier-free theory of word equations, length constraints and membership predicate over regular expressions is also decidable. They also studied string constraints generated by the Kudzu JavaScript bugfinding tool [Saxena et al. 2010], and found that most word equations that occur in practice are either already in solved form or can be algorithmically converted into one.

Another interesting result proved independently by multiple authors [Marchenkov 1982; Durnev 1995; Ganesh et al. 2011] is the undecidability of the validity problem for ∀∃-sentences over positive word equations (AND-OR combination of word equations without negation). These are currently the strongest undecidability results for any theory involving word equations.

All the above-mentioned theoretical work is for theories where the string variables range over an infinite domain of strings. In their recent work, Jha et al. [2009]

showed that the theory of word equations over finite-length strings with substring operation, concatenation, and extraction is NP-complete. This work builds on the NP-completeness result that we obtained for the satisfiability problem for HAMPI's logic.

7. CONCLUSION

We presented HAMPI, a solver for constraints over fixed-size string variables. HAMPI constraints express membership in regular and fixed-size context-free languages. HAMPI constraints may contain a fixed-size string variable, context-free language definitions, regular-language definitions and operations, and language-membership predicates. Given a set of constraints over a string variable, HAMPI outputs a string that satisfies all the constraints, or reports that the constraints are unsatisfiable. HAMPI works by encoding the constraint in the bit-vector logic and solving using STP.

HAMPI is designed to be used as a component in testing, analysis, and verification applications. HAMPI can also be used to solve the intersection, containment, and equivalence problems for regular and fixed-size context-free languages. We evaluated HAMPI's usability and effectiveness as a component in static- and dynamic-analysis tools for PHP Web applications. Our experiments show that HAMPI is expressive enough to easily encode constraint arising in finding SQL injection attacks, and in systematic testing of real-world programs. In our experiments, HAMPI was able to find solutions quickly, and scale to practically-relevant problem sizes.

By using a general-purpose freely-available string-constraint solver such as HAMPI, researchers in program analysis, formal methods, testing and software engineering can save significant development effort, and improve the effectiveness of their tools.

The power of bounding. HAMPI accepts only bounded languages. All bounded languages are finite, and all finite languages are regular. Hence, it would suffice to say that HAMPI supports only bounded regular languages. However, it is important to emphasize the ease-of-use that HAMPI provides by allowing users to use context-free languages as input. Furthermore, our experiments show how powerful bounding can be. For many applications, bounding the input language (whether it be regular or context-free or context-sensitive languages or even Turing-complete languages) enables creation of powerful and expressive tools. The cost of bounding is often limited, since for many applications a bounded logic is sufficient to express the associated constraint satisfaction problem. The power of bounding has been known to researchers in related areas, such as bounded model-checking. We foresee that powerful solvers for bounded versions of expressive logics will be created in the near future, and that they will help the applications of formal methods to software engineering problems.

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